

# ***Applications of Artificial Intelligence***

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## **Chapter 4:** Knowledge-Based Systems

### 4.3: Model-Based Reasoning **Details**

# Model-Based Diagnosis (MDS)

## Terminology of the GDE approach:

### Component:

Unit of which behaviour should be classified („diagnosed“)  
usually enumerated from 1 to n

### Component type:

collects components of same behaviour

### Behavioural mode:

represents a specific behaviour of all components of that type  
usually enumerated from 1 to k:

1 represents ok

2 thru k are the fault modes (ordered by probability)

### (Diagnosis) Candidate:

Assignment of exactly one behavioural mode to each component of the system

# Model-Based Diagnosis (MDS)

## Terminology of the GDE approach:

### Candidate:

(2 1 3 1 1 2 1) means:

- Component Nr. 1 is in behavioural mode 2
- Component Nr. 2 is in behavioural mode 1
- Component Nr. 3 is in behavioural mode 3
- Component Nr. 4 is in behavioural mode 1
- Component Nr. 5 is in behavioural mode 1
- Component Nr. 6 is in behavioural mode 2
- Component Nr. 7 is in behavioural mode 1

### Conflict:

Assignment of exactly one behavioural mode to some components of the system

(0 1 0 0 0 2 0) means:

- Component Nr. 2 is in behavioural mode 1
- Component Nr. 6 is in behavioural mode 2
- About the other components no proposition is made.

**Interpretation:** It is not consistent that component 2 is in behavioural mode 1 and und component 6 is in behavioural mode 2.

# Model-Based Diagnosis (MDS)

## Terminology of the GDE approach:

### Diagnosis (= consistent candidate):

Candidate not containing any conflict

Examples:  $(2\ 1\ 3\ 1\ 1\ 2\ 1)$  contains the conflict  $(0\ 1\ 0\ 0\ 0\ 2\ 0)$ , i.e., it is not a diagnosis.

If  $(0\ 1\ 0\ 0\ 0\ 2\ 0)$  is the only conflict, then  $(1\ 1\ 1\ 1\ 1\ 1\ 1)$  is a diagnosis.

If  $(0\ 1\ 0\ 0\ 0\ 2\ 0)$  and  $(1\ 1\ 0\ 0\ 0\ 0\ 0)$  are the only conflicts, then  $(1\ 2\ 1\ 1\ 1\ 1\ 1)$  is a diagnosis

### Preference between candidates:

A candidate A is preferred to another candidate B, if A assigns at most the number of the behavioural mode of B for each component.

Example:  $(1\ 1\ 1\ 1\ 1\ 1\ 1)$  is preferred to  $(1\ 2\ 1\ 1\ 1\ 1\ 1)$

### Maximum preferred diagnosis:

A diagnosis is called a maximum preferred diagnosis, if all preferred candidates contain conflicts, i.e. the diagnosis is maximum with respect to the preference relation.

Example: If  $(0\ 1\ 0\ 0\ 0\ 2\ 0)$  and  $(1\ 1\ 0\ 0\ 0\ 0\ 0)$  are the conflicts, then  $(1\ 2\ 1\ 1\ 1\ 1\ 1)$  and  $(2\ 1\ 1\ 1\ 1\ 1\ 1)$  are the only two maximum preferred diagnoses.

# Model-Based Diagnosis (MDS)

**Goal of MDS (Daimler enhancement of the GDE):**

- 1) **Base functionality:** Find the best diagnoses
- 2) **Extended functionality:** Repair instruction:  
Propose actions and tests in order to distinguish between diagnoses found in 1)

**Details of 1): Find the maximum preferred diagnoses.**

If there are too many maximum preferred diagnoses, the focus should be restricted to the *most probable* ones among *all* maximum preferred diagnoses.

The remaining maximum preferred diagnoses are to be marked as *pending* and may be inserted into focus at a later time.

Possible focus restriction policies (may be combined):

- a) Determine a maximum number of focus diagnoses
- b) Determine a probability threshold for the gap between focus diagnoses and pending diagnoses.

# Model-Based Diagnosis (MDS)

Algorithm for finding the most probable maximum preferred diagnoses  
(**Problem 1**):

At any time, all candidates of the focus are maximum preferred.

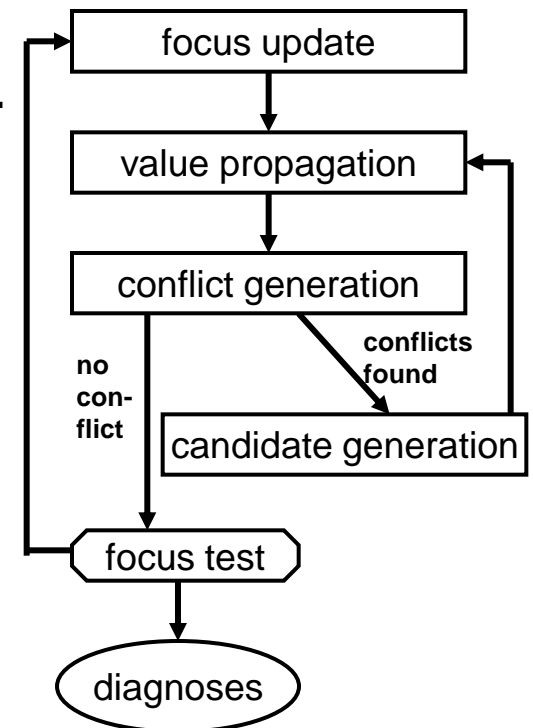
1. **Update the focus candidates:** Initialise with 11....1.  
At later stages, pending candidates may be dragged into focus.
2. **Generate and propagate all values resulting from behavioural modes of candidates in focus.**
3. **Find the minimal conflicts from the propagated values.**
4. **Exclude the candidates containing conflicts and compute new maximum preferred candidates not containing any conflict.**
5. **If focus is sufficiently large, the goal is achieved.**  
Otherwise continue with 1.

*In reality, steps 2 thru 4 are implemented concurrently.*

**(achieved by event oriented programming)**

In the following, the methods for **candidate generation** and **conflict generation** are described separately.

## *Diagnostic cycle*



# MDS: Candidate generation

## INPUT:

- **Old conflicts and all maximum preferred und consistent diagnoses for these conflicts**
- **New conflicts**

## OUTPUT:

- **Set of maximum preferred candidates being consistent for the new conflicts, too**

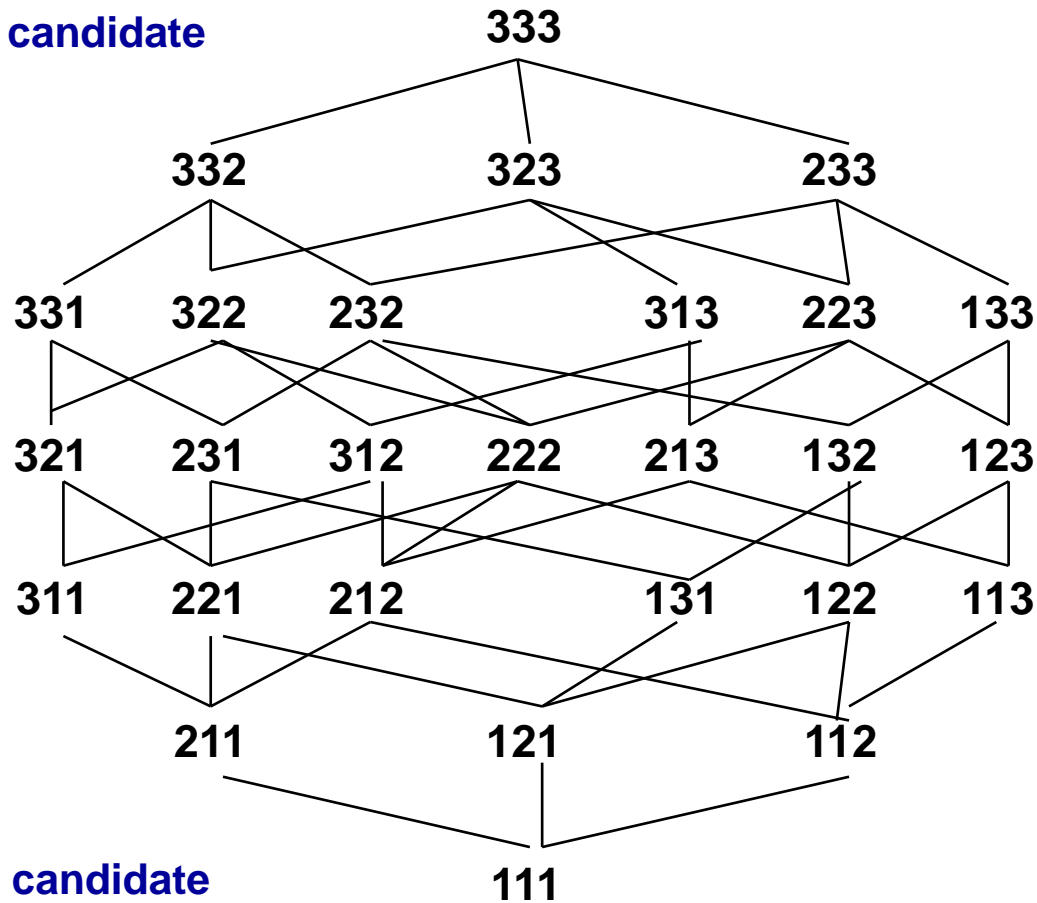
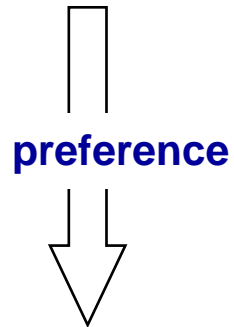
## Embedding the candidate generation into the diagnostic process:

- Output of candidate generation will be taken as input in the next diagnostic cycle.
- Value propagation may find new conflicts.
- New conflicts may kick out diagnoses from focus.
- If no new conflicts are found, the diagnostic process is finished.

# MDS: Preference web of candidates

**Example:** 3 components  
3 behavioural modes for each of the components

minimum preferred candidate

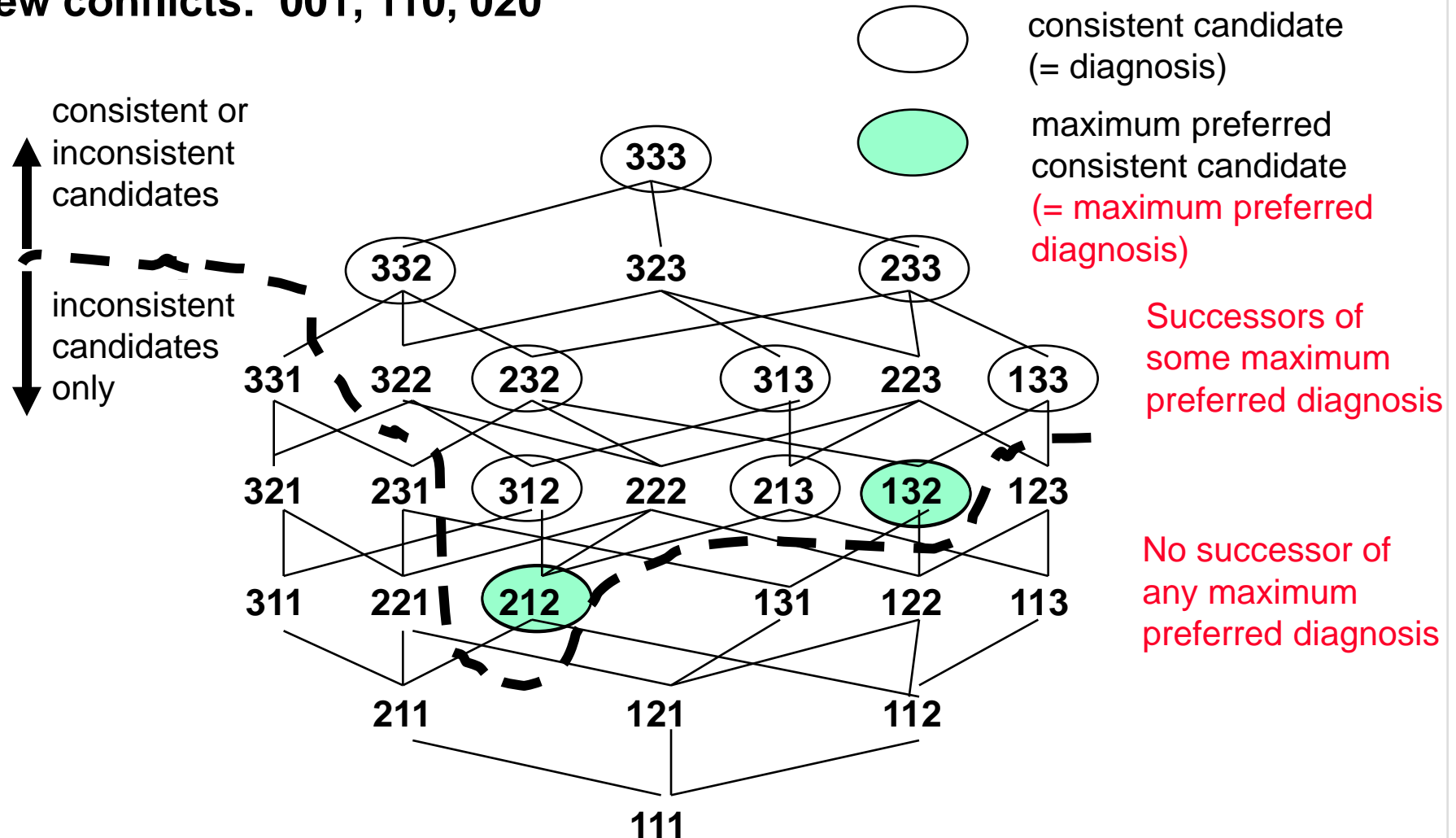


maximum preferred candidate



# MDS: Preference web of candidates

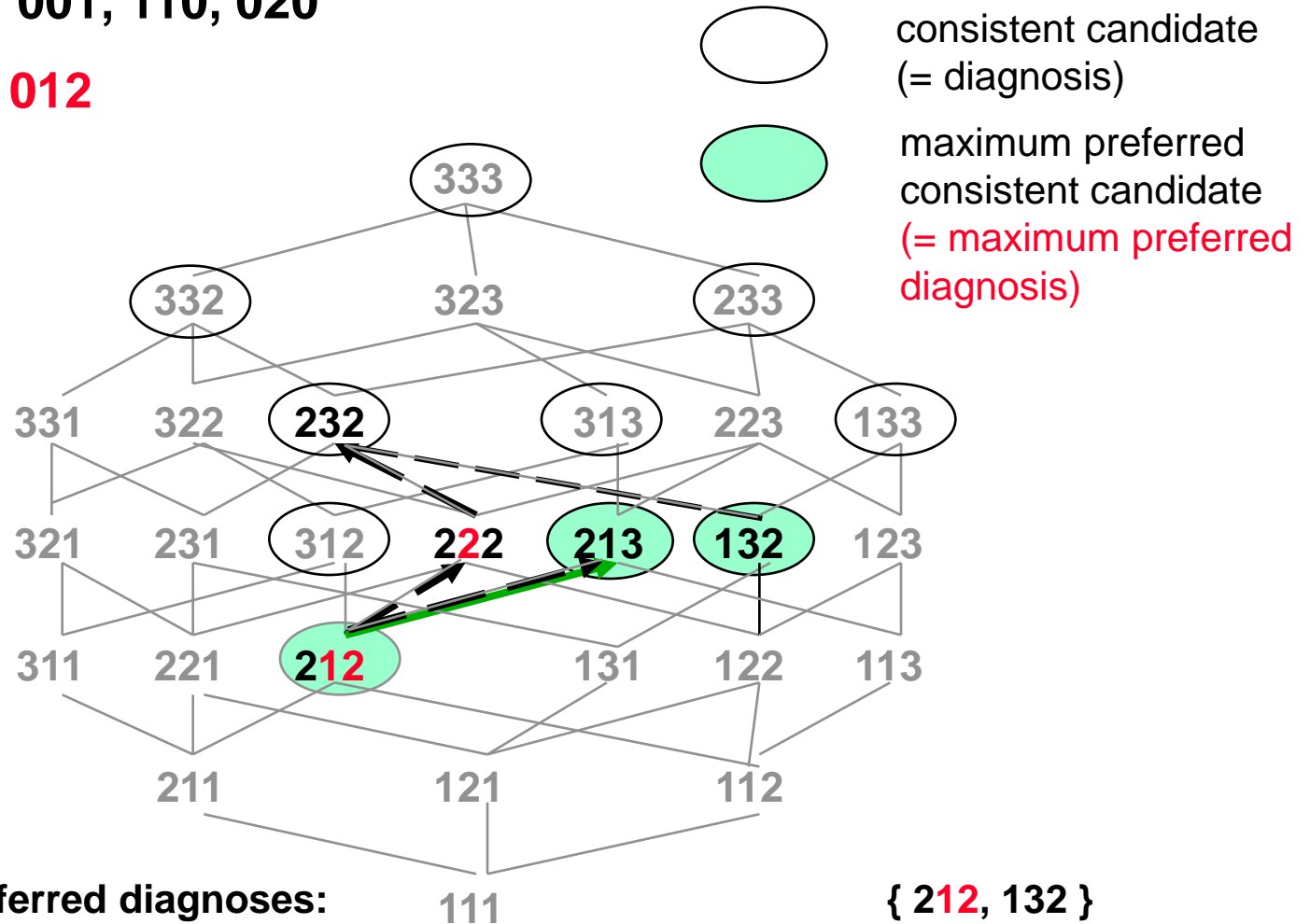
New conflicts: 001, 110, 020



# MDS: Candidates update

Old conflicts: 001, 110, 020

New conflict: 012



Former maximum preferred diagnoses:

111

{ 212, 132 }

New maximum preferred diagnoses (stage 1):

{ 222, 213, 132 }

New maximum preferred diagnoses (stage 2):

{ 213, 132 }

# MDS: Candidates update

## Actions at detection of a new conflict:

- 1) Consistency check of all maximum preferred diagnoses
- 2) Removal of all candidates proven to be inconsistent
- 3) Generation of the preference successors of each candidate just removed
- 4) Adopting the preference successors satisfying the following conditions:
  - The successor is not preferred by a different consistent diagnosis.
  - The successor is consistent itself.

# MDS: Candidates update

## Actions at detection of a new conflict :

3) Generation of the preference successors of each candidate just removed:

- If C is a conflict contained in an old diagnosis, then generate only successors of C changing the behavioral mode of **just one component contained in C**.

(Generation of direct successors only, directly referring to conflict C)

***Remark: This restricted method does not skip any eventual diagnosis***

***Prop.:*** Each successor diagnosis not containing C is successor diagnosis of a direct successor not containing C

- If one of the direct successors contains a conflict C', then do not generate this successor, but rather all successors referring directly to C'.

# MDS: Optimising the candidate generation

## Eliminating **irrelevant** conflicts:

- Conflicts are only relevant, if they may eventually remove a successor of a presently maximum preferred diagnosis.
- For the consistency test, only consider relevant conflicts: Each diagnosis  $d$  stores the relevant conflicts. Any successor of  $d$  will only be checked for the conflicts of  $d$ 's list.

## Examples for relevant conflicts:

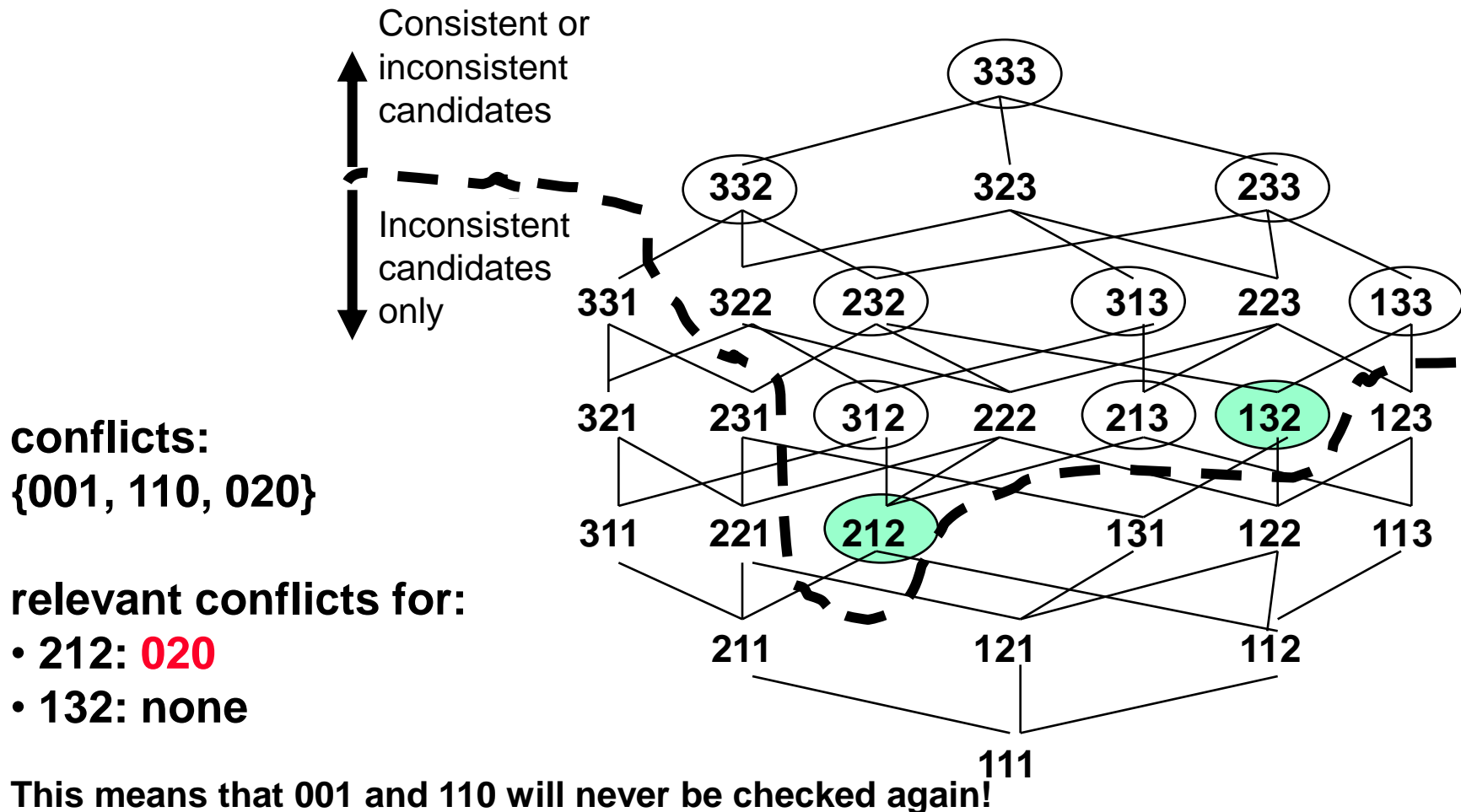
conflict:	0 2 2	2 0 2	2 0 2
candidate:	3 1 2	2 1 1	1 1 3
relevant ?			

## Mathematical criterion for the relevance of a conflict (easy to check!)

A conflict  $c$  is relevant for a diagnosis  $d$  if for all components holds:  
 $c$  either assigns no mode (0) or a mode at least as high as the mode in  $d$ .

# MDS: Optimising the candidate generation

## Eliminating **irrelevant** conflicts:



# MDS: Optimising the candidate generation

**The Daimler product MDS contains a lot of further optimisations for accelerating the candidate generation process which are not mentioned here.**

# MDS: Conflict generation

## Candidate generation solves the following task:

- **Given a set of conflicts: Find the most probable maximum preferred diagnoses taking into account those conflicts.**
- **This reduces the problem of finding the best diagnosis to the following task: Find the set of conflicts !**

## What is a conflict ?

- **Assignment of exactly one behavioural mode to some component of a system**
- **Logically, a conflict is a disjunction of negative literals.**
- **Comparing: Logically, a diagnosis is a conjunction of positive literals.**

## How is a conflict generated?

- **by values contradicting each other**
- **The contradicting values are backed by different assumptions.**
- **Then one of the assumptions must be false.**



# TMS: Truth Maintenance System

## Objects of a TMS:

### Propositional node:

Represents an arbitrary proposition (may be true or false)

### Justification:

$A_1 \wedge A_2 \wedge \dots \wedge A_n \Rightarrow C$      where  $A_1, A_2, \dots, A_n, C$  are propositional nodes

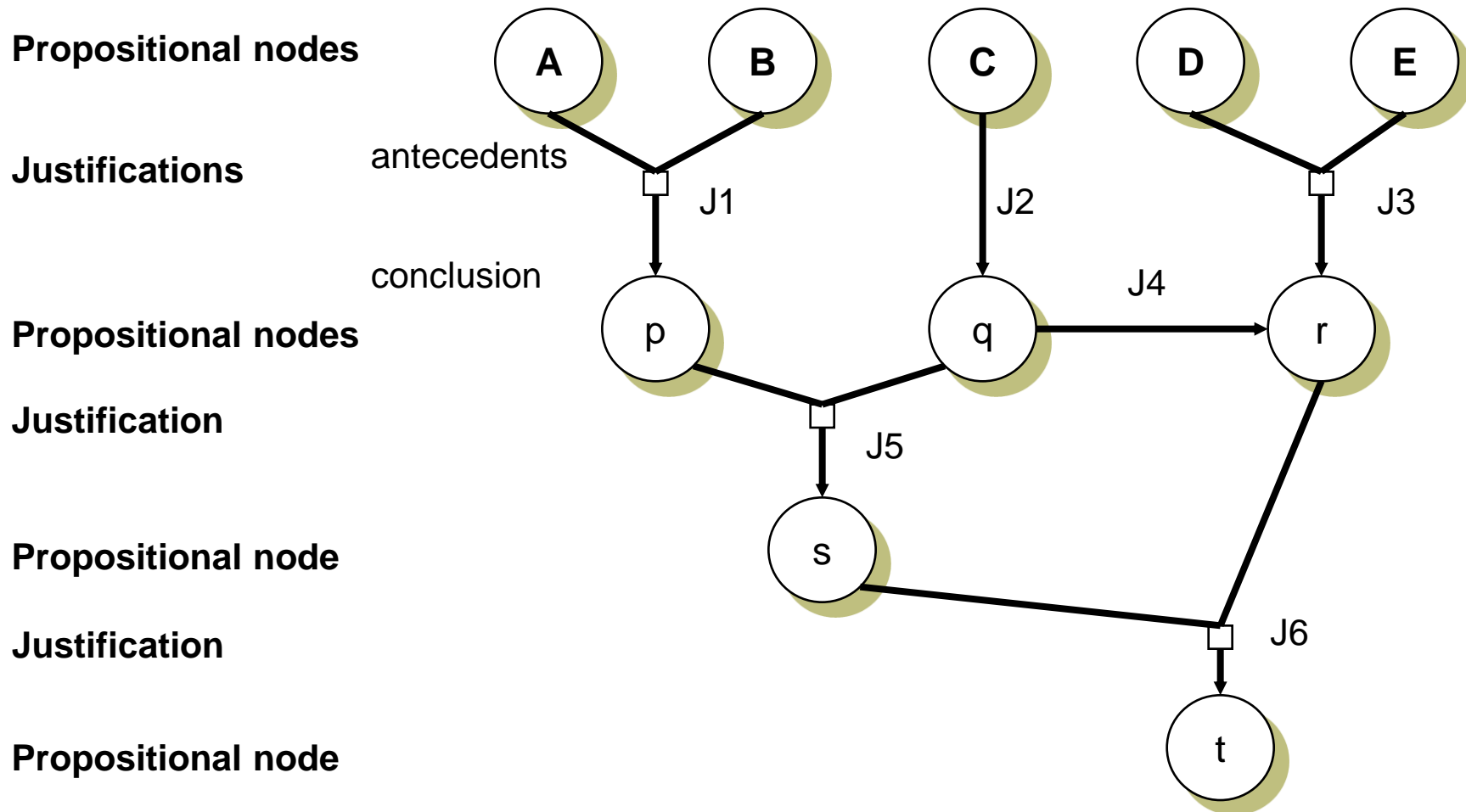
$A_1, A_2, \dots, A_n$  are the **antecedents** of the justification

$C$  is the **conclusion** of the justification

### Contradiction node ( $\perp$ ):

represents a proposition which holds by no means

# TMS: Truth Maintenance System



**From the combination of propositions,  
a justification makes a new proposition.  
The antecedents of a justification are to be considered as conjunction.**

# ATMS: Assumption-based Truth Maintenance System

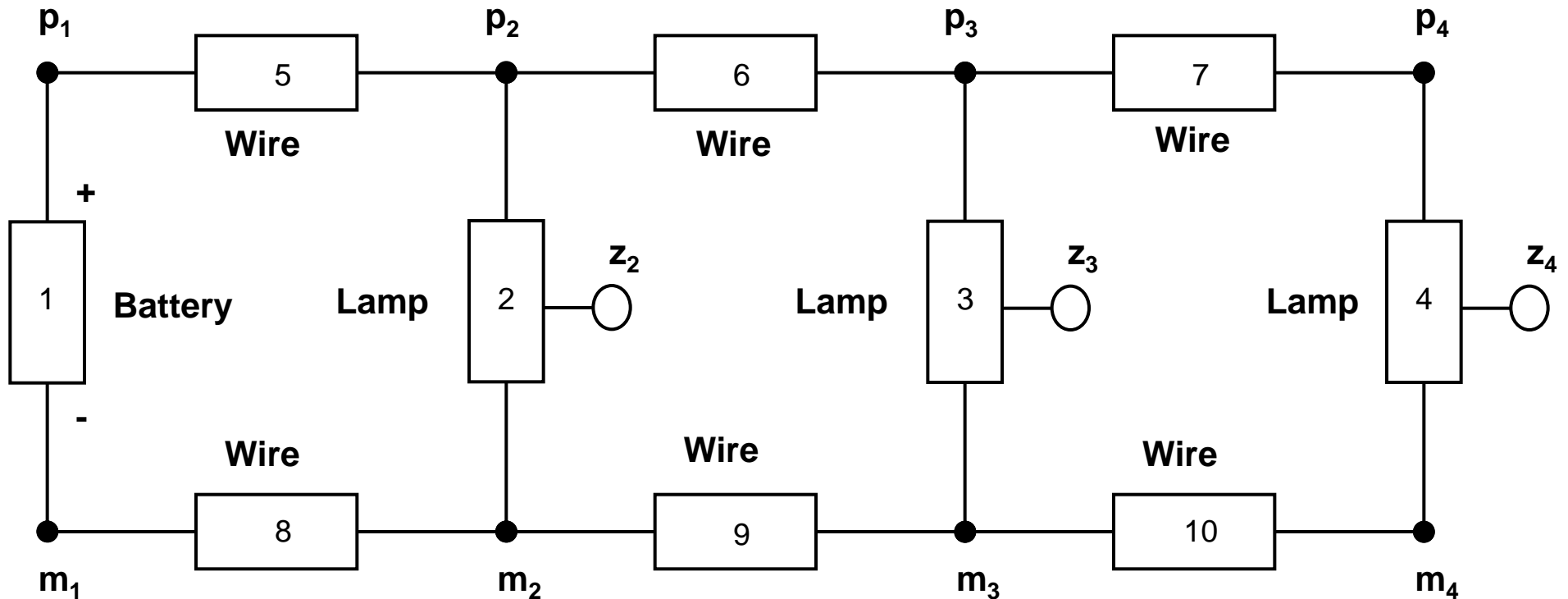
## Functionality of a **general** TMS:

- 1) Certain propositional nodes are considered true (beliefs).
- 2) TMS determines by propagation of these assumptions via the justifications which other propositions must also hold then.
- 3) In particular, if the contradiction node must hold, then the assumptions must be contradictory.

## Additional functionality of an **A**TMS:

- An ATMS works with *several* assumption sets in parallel: A (context) environment is the set of assumptions that should hold at the same time, but there may be different such environments holding alternatively.
- 1) The propositions are assigned with the assumption environments under which they must hold.
  - 2) The ATMS propagates these assumption environments over the justifications and determines which other propositions must hold then as well.
  - 3) In particular, the environments of the contradiction node reveals which environments are contradictory.

# Example for applying an ATMS



## Behavioural modes:

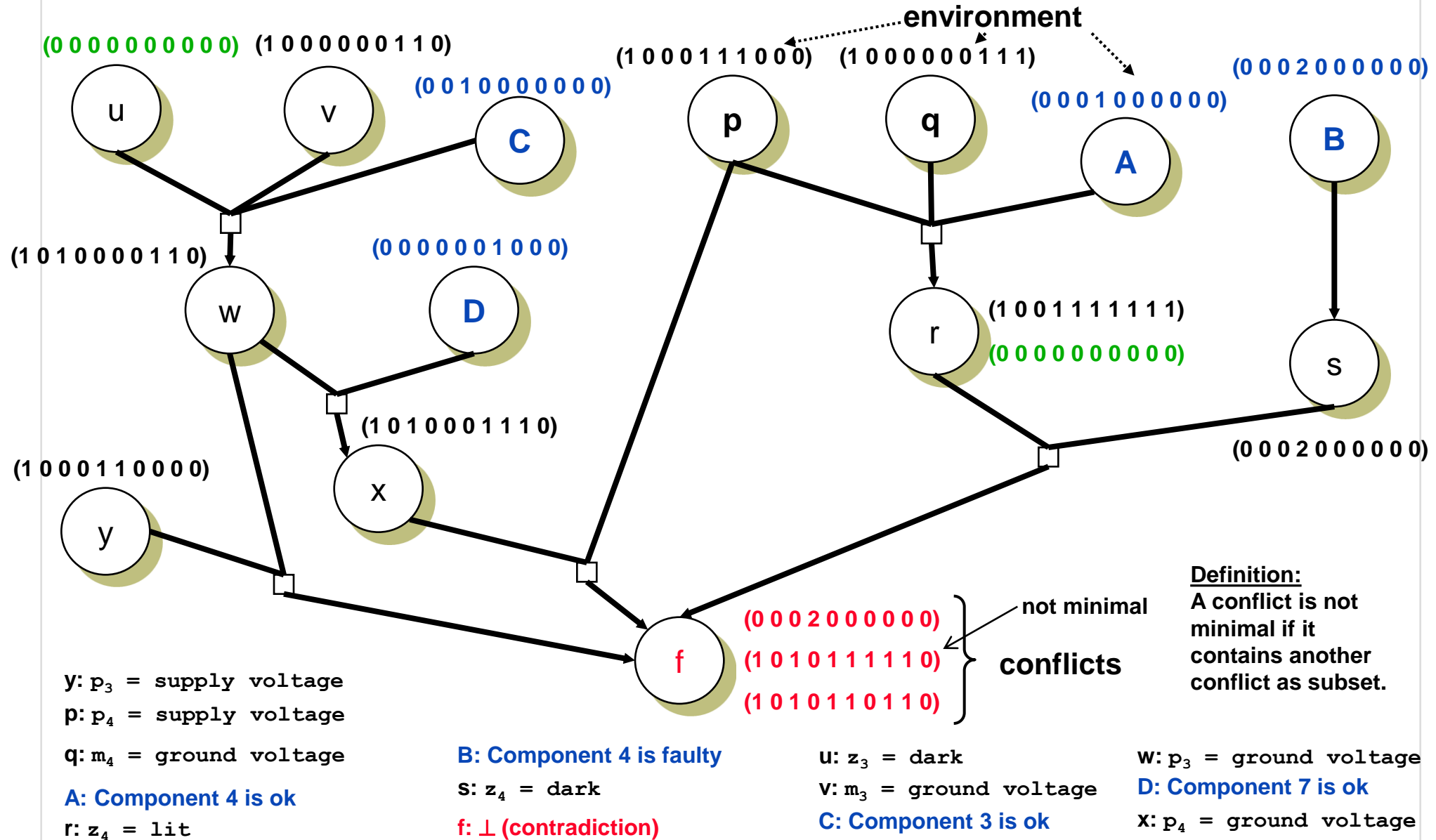
Mode 1 for all component types: normal behaviour

Modus 2 for all component types: unique fault mode

**Battery:** Modus 2  $\Rightarrow$  (minus = ground voltage)

**Lamp:** Modus 2  $\Rightarrow$  (z = dark)

# Example for applying an ATMS



# ATMS: Assumption-based Truth Maintenance System

## Terminology of ATMS:

### Propositional node:

The propositional nodes distinguish between *normal propositions* and *assumptions*, i.e. the class of assumption nodes is a specialisation of propositional nodes.

### Environment:

Context of assumptions: *Conjunction* of assumptions, under which a proposition holds (if all assumptions of this environment are valid)

### Label:

Set of different environments for a propositional node. Different environments need not be consistent to each other. The proposition holds already under the *disjunction* of the environments.

### conflict (nogood):

Environment of the label of the contradictory node

# ATMS: Assumption-based Truth Maintenance System

## Application of an ATMS for model-based diagnosis:

### Propositional nodes:

- 1) „Normal“ nodes: Assignment of a certain value to a certain position (variable) in the system
- 2) Assumption node: Assignment of a behavioural mode to a component

**Justification:** Application of a generic behavioural rule to actual values

### Environment:

Concurrent (conjunction) assignment of behavioural modes to components under which a proposition would hold. The assignment need not be complete, i.e. it is an arbitrary candidate (like in a conflict).

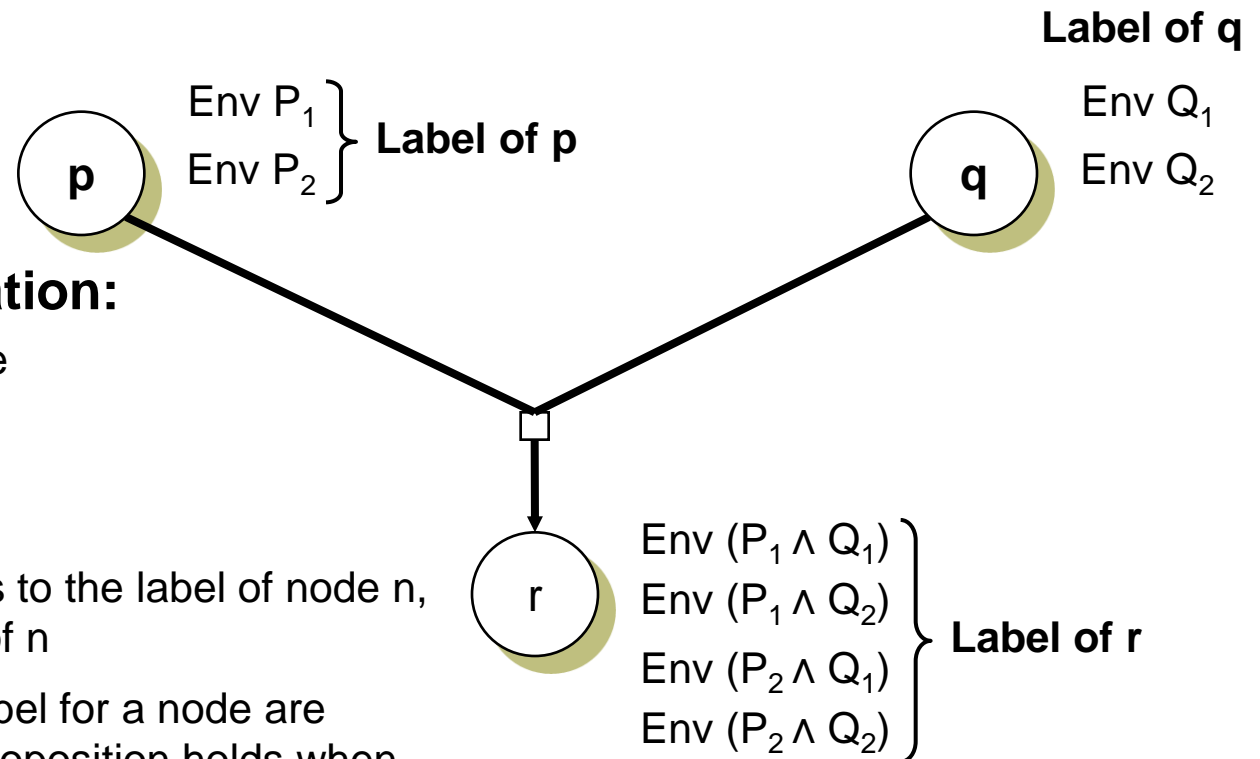
For assumption nodes: Assignment of a behavioural mode to exactly one component

### conflict (nogood):

Environment of the label of the contradictory node: Assignment of behavioural modes to components of which at least one must be faulty.

***This enables the same notation and meaning of conflicts as in the terminology of the GDE.***

# Label update in an ATMS



## Interpretation of justification:

- $r$  holds when  $q$  and  $p$  are true (conjunction)

## Interpretation of labels:

- When environment  $e$  belongs to the label of node  $n$ , this means:  $e \Rightarrow$  proposition of  $n$
- Several environments of a label for a node are treated as disjunction: The proposition holds when at least one of the environments is true.

## Elimination of redundant environments:

- Contradictory environments may be removed.
- This enables the removal of all environments containing conflicts.
- Environments implying other environments of the same label may be omitted as well.



# User interface of an ATMS

## Input of problem solver:

- Assumption nodes
- “Normal” nodes
- Justifications between the nodes  
(they must be obtained from the component library applied to actual values)
- Certain environment assignments to normal nodes,  
e.g., observations or other premises as (0 0 ... 0)

## Output to the problem solver:

- Set of minimal conflicts (Definition of minimality on slide 21)

## The ATMS performs automatically: *These are a lot of operations !*

- Generation of labels for the assumption nodes
- Update of labels for all conclusions where the label of some antecedent has changes.
- Elimination of redundant environments

# User interface of an ATMS

## Input of problem solver:

- Assumption nodes
- “Normal” nodes
- Justifications between the nodes  
(they must be obtained from the component library applied to actual values)
- Certain environment assignments to normal nodes,  
e.g., observations or other premises as (0 0 ... 0)

## Output to the problem solver:

- Set of minimal conflicts

## Interaction with the candidate generator:

- Generate all assumption nodes for the focus diagnoses
- Value propagation (simulation):  
Compute all values resulting from assumptions of the focus diagnoses,  
generate the respective propositional nodes und justifications,  
plug this into the ATMS.
- Ask the ATMS for the new conflicts.

# Value propagation and ATMS

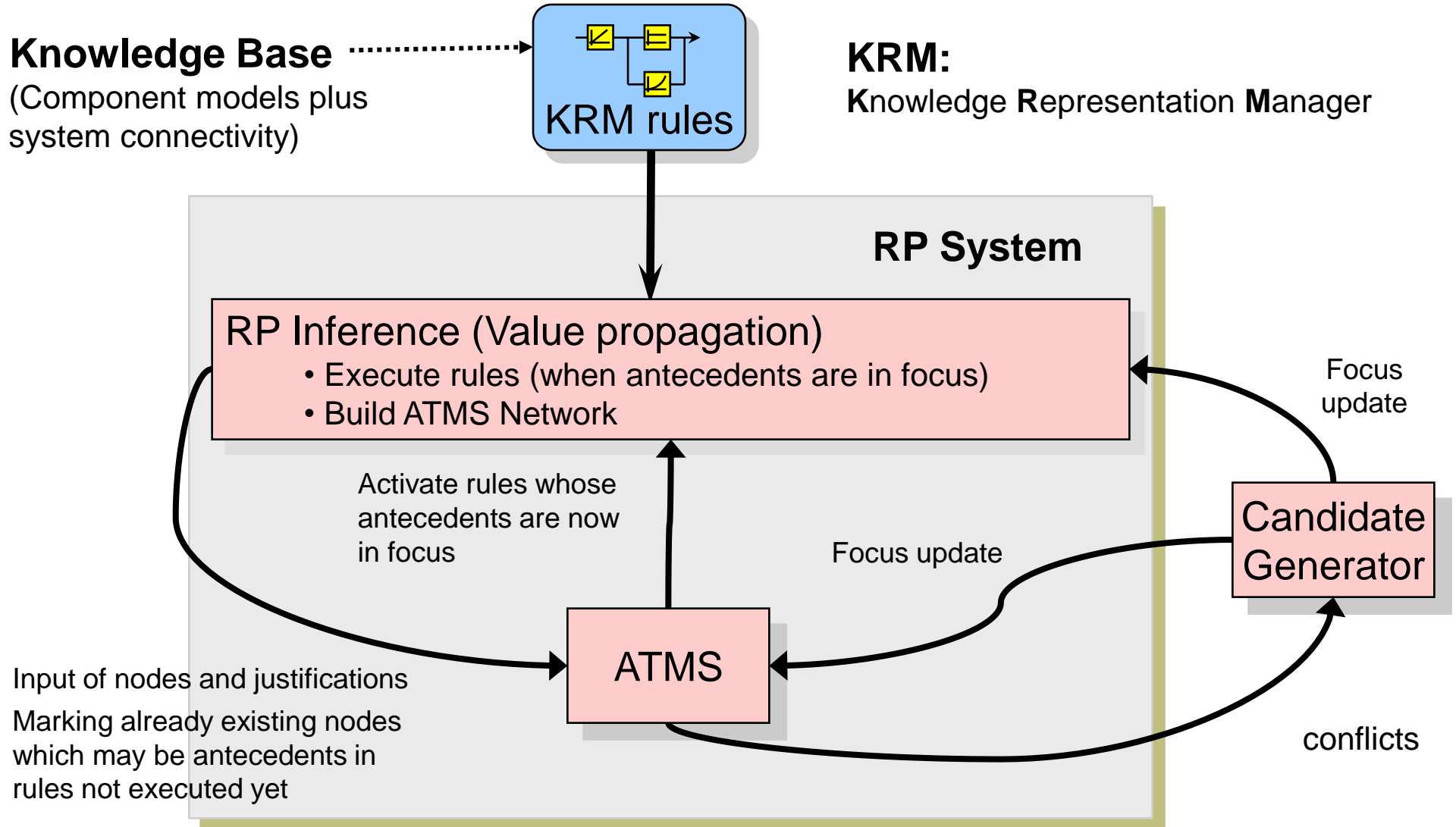
## What is propagation in general ?

- Propagation is the distribution of information in a network made of nodes and edges

## Separation of value propagation (RP) and ATMS:

- The **ATMS** is responsible for *propagation of environments* in a given network with already determined value dependencies.
- The *propagation of values* is performed by a rule propagator (**RP**) which generates justifications for actual values from the generic values of the behavioural modes of the components. Thus, RP generates the network of value dependencies required by the ATMS.

# Value propagation and ATMS



*In optimised candidate generators and ATMS's the interface is more complicated.*

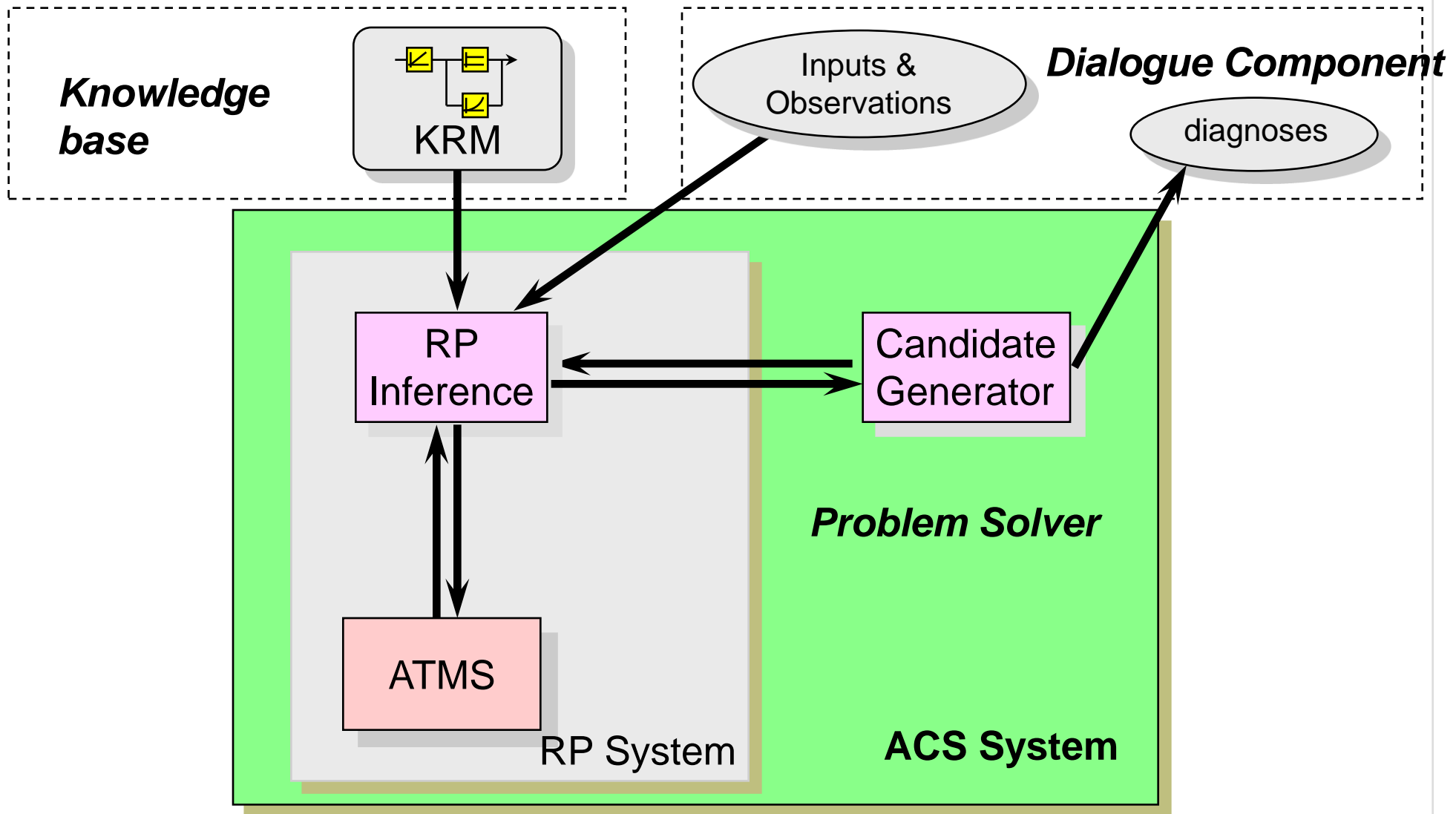
# Value propagation and ATMS

## What is the benefit of separating value propagation and ATMS?

### → Better software architecture by modularisation

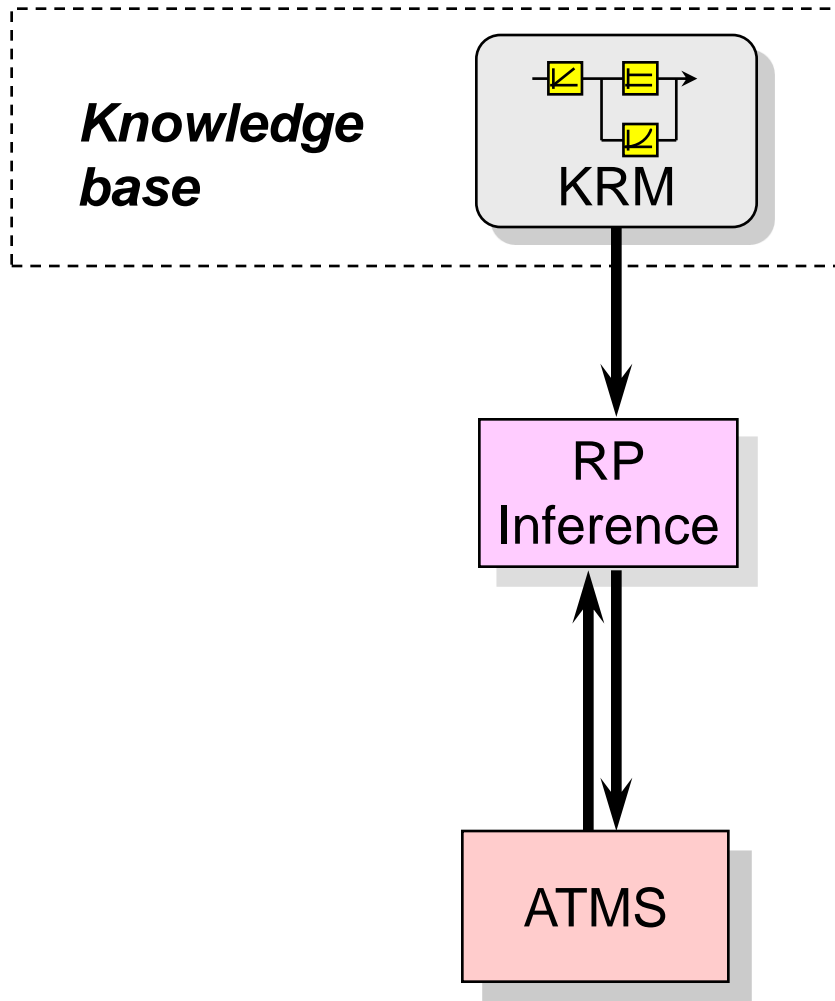
- **Values** are generated mostly from observations (measurements) and intended actions. This is not frequent, thus, there are **not many** values to be considered.
- **Environments** are generated from assumptions about behavioural modes. Of such constructs there exist **a lot of** (even at single faults at least as many as there exist components).
- This makes the update of focus environments much more often to occur than the computation of new values. The update of focus environments may be considered an ATMS internal problem

# Interaction of candidate generator, RP and ATMS



**ACS: Assumption-based Constraint Solver**

# Requirement to the knowledge base



**What does the knowledge base have to provide to the inference component (problem solver)?**

- Rules for the relations of values in each behavioural mode (*component models*)
- Knowledge about the value domains:  
When are two values considered contradictory?

***Daimler's MDS solves these requirements by offering a constraint language for component models.***