# **Algorithmics** Sebastian Iwanowski FH Wedel 5. String Matching

# **Algorithmics 5**

## **String Matching**

**Task:** Given a text  $T = \{t_1, ..., t_n\}$  with n literals and a pattern  $P = \{p_1, ..., p_m\}$  with m literals:

Find the starting positions where P occurs in T.

**naive algorithm:** needs O(nm) time

Algorithm of Knuth-Morris-Pratt: needs O(n) time

**Def.:**  $P_q$  denotes the prefix of P consisting of the first q literals.  $(P_q = P[1],...,P[q])$ 

**Def.:** The prefix function  $\pi: \mathbb{N}\setminus\{0\} \to \mathbb{N}$  for the pattern P is defined as:

 $\pi(q) = k \Leftrightarrow k$  is the length of the longest strict prefix of  $P_q$  (*strict* means: k < q)

which is also a Suffix of P<sub>a</sub>

### **General method of the KMP algorithm:**

For each  $q \le m$ , compute the value  $\pi(q)$  of the prefix function and store it. Then scan T in only one iteration and shift P at any mismatch in pattern position q by  $q - \pi(q)$ .

### References:

Alt, Kap. 4.8

Cormen, ch. 32 (String matching), esp. 32.4 (KMP)

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## **String Matching**

Algorithm of Knuth-Morris-Pratt: needs O(n) time

Implementation of main procedure:

```
i := 1; q := 0;
                               .... Invariant: q=0: no strict prefix of P coincides at a suffix of P ending at i
while i \leq n do
                                             g>0 corresponds to the maximum index < i s.t.
                                             (P[i-q+1],...,T[i]) coincides with (P[1],...,P[q])
    while (q>0) and (T[i] \neq P[q+1])
        q := \pi (q);
     if T[i] = P[q+1] then q := q+1;
     if q = m
        then
              print ("Matching at position ", i-m);
              q := \pi (q);
                                                 In class: Why is this algorithm correct?
     i := i+1;
                                                 Home work:
                                                 Why does this algorithm need O(n) time?
```

#### References:

Alt, Kap. 4.8 Cormen, ch. 32 (String matching), esp. 32.4 (KMP)

# **Algorithmics 5**

## **String Matching**

Algorithm of Knuth-Morris-Pratt: needs O(n) time

Implementation of prefix function (according to Cormen/Alt): needs O(m) time

Invariant: q=0: no strict prefix of P coincides at a suffix of T ending at i q>0 corresponds to the maximum index < i s.t. (P[i-q+1],...,P[i]) coincides with (P[1],...,P[q])

In class: Why is this algorithm correct?

In class:

Why does this algorithm need O(m) time?

#### References:

Alt, Kap. 4.8 Cormen, ch. 32 (String matching), esp. 32.4 (KMP)