

## ECDSA Signing Steps in Detail:

(see e.g. Paar, Pelzl, "Understanding Cryptography", Springer Heidelberg 2010, ISBN 978-3-642-04100-6)

- 1. Chose** a secret ephemeral key  $k_e$   
(Use a secure and properly initialized Pseudo Random Number Generator to generate an Integer  $k_e$  smaller than, but of same bytelength as domain group order  $q$ .)
- 2. Calculate**  $k_e^{-1}$  using the Chinese Remainder Theorem.
- 3. Calculate** point  $R = k_e \cdot A$   
(A is the domains primitive point generating the group.)
- 4. Select** x-component of Point  $R$  and denote it as " $r$ ".
- 5. Compute** hash value  $hash$  of file to be signed.
- 6. Provide** secret private key  $d$
- 7. Calculate**  $s = \left( (hash + d \cdot r) \cdot k_e^{-1} \right) \bmod q$
- 8. Create signature file** containing a *domain identifier* with *hash specifier* for information and the signature components  $r$  and  $s$ .

## ECDSA Signature Verification Steps in Detail:

- 1. Retrieve** signers public Key  $B$  from a trusted source and  $r$ ,  $s$  from signature file.
- 2. Retrieve** parameters of domain used by signer (got domain id from signature file).
- 3. Calculate** auxiliary value  $w = s^{-1} \bmod q$ .
- 4. Calculate** auxiliary value  $u1 = (w \cdot hash) \bmod q$ . (Hash algorithm specified in signature file.)
- 5. Calculate** auxiliary value  $u2 = (w \cdot r) \bmod q$ .
- 6. Compute** point  $P = u1 \cdot A + u2 \cdot B$ .
- 7. Accept** signature if x-component of  $P$  equals  $r$ :  $(x_P \equiv r) \bmod q$ ,  
reject otherwise.